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Accurate Values of the Exponent Governing Potential Flow about Semi-Infinite Cones

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IT is well known that, for axisymmetric, inviscid, and incompressible flow about a semi-infinite cone, the velocity V on the surface of the cone varies with the distance s from the vertex in the following manner:

$$V = Cs^m \quad (1)$$

where C is simply a scaling constant. The flow is thus completely characterized by the exponent m , which is a function of Θ , the semivertex angle of the cone. Tabulated values of m do not appear to be readily available in the literature. Reference 1 gives a small graph of m vs Θ and also lists three references, including the original work of Ref. 2. However, none of the three is contained in ordinary technical libraries.

The equation relating m and Θ is

$$P_{m+1}'(-\cos\Theta) = 0 \quad (2)$$

where the prime denotes differentiation and the function

Table 1 Values of the exponent governing potential flow about semi-infinite cones

| Θ , deg | m | Θ , deg | $1/m$ |
|----------------|-----------|----------------|-----------|
| 0 | 0.0000000 | 90 | 1.0000000 |
| 5 | 0.0037441 | 95 | 0.8779641 |
| 10 | 0.0145329 | 100 | 0.7715075 |
| 15 | 0.0316314 | 105 | 0.6779398 |
| 20 | 0.0544316 | 110 | 0.5951432 |
| 25 | 0.0825162 | 115 | 0.5214293 |
| 30 | 0.1156458 | 120 | 0.4554368 |
| 35 | 0.1537334 | 125 | 0.3960580 |
| 40 | 0.1968232 | 130 | 0.3423826 |
| 45 | 0.2450773 | 135 | 0.2936569 |
| 50 | 0.2987690 | 140 | 0.2492515 |
| 55 | 0.3582834 | 145 | 0.2086375 |
| 60 | 0.4241237 | 150 | 0.1713675 |
| 65 | 0.4969244 | 155 | 0.1370604 |
| 70 | 0.5774709 | 160 | 0.1053903 |
| 75 | 0.6667277 | 165 | 0.0760764 |
| 80 | 0.7658769 | 170 | 0.0488761 |
| 85 | 0.8763705 | 175 | 0.0235785 |
| 90 | 1.0000000 | 180 | 0.0000000 |

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P_{m+1} is the Legendre function that remains finite when its argument equals unity for all values of its order $m+1$ (see Ref. 3). Using the series expansion of P_{m+1} , this equation was solved numerically for m at values of Θ ranging from 0° to 180° by 5° increments. The results are given in Table 1.

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Variable Collision Frequency Effects on Hall-Current Accelerator Characteristics

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Nomenclature

| | |
|----------------|---|
| B | = magnetic induction |
| b | = ion-slip parameter |
| E | = electric field |
| e | = charge on electron |
| J | = current density |
| L | = reference length |
| M | = Mach number |
| m | = mass flow |
| m_a | = atom mass |
| N | = interaction parameter |
| P | = pressure |
| S | = parameter defined by Eq. (4) |
| T | = temperature |
| V | = velocity |
| z' | = dimensionless axial coordinate = z/L |
| α | = degree of ionization |
| β | = Hall parameter defined by Eq. (5) |
| γ | = specific heat ratio |
| η | = energy conversion efficiency |
| ρ | = mass density |
| σ | = electrical conductivity |
| τ | = time between collisions |
| $\bar{\tau}_e$ | = mean electron collision time |
| ϕ | = voltage difference between inlet and exit |
| ω | = cyclotron frequency |

Subscripts

| | |
|----------|---------------------------|
| ei | = electron-ion collision |
| ea | = electron-atom collision |
| ia | = ion-atom collision |
| 0 | = accelerator inlet |
| z | = axial direction |
| θ | = azimuthal direction |

ONE-dimensional magnetogasdynamic (MGD) analyses of the coaxial Hall-current accelerator have recently been presented by Brandmaier, Durand, Gourdine, and Rubel¹ and by Cann and Marlotte.² Each considered the steady continuum flow of an ideal, electrically neutral, slightly ionized, three-species gas mixture through a narrow constant

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